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Journal of Catalysis 240 (2006) 73–84

**JOURNAL OF CATALYSIS** 

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# A comprehensive density functional theory study of ethane dehydrogenation over reduced extra-framework gallium species in ZSM-5 zeolite

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Received 5 December 2005; revised 20 March 2006; accepted 20 March 2006

# **Abstract**

The stability of various gallium species  $(Ga^+, GaH_2^+,$  and  $GaH_2^{+2})$  as models for the active sites in reduced  $Ga/ZSM-5$  and the possible reaction paths of alkane dehydrogenation were studied using a density functional theory cluster modeling approach. In general, alkanes are preferentially activated via an "alkyl" mechanism, in which gallium acts as an acceptor of the alkyl group. A comparison of the computed energetics of the various reaction paths for ethane indicates that the catalytic reaction most likely proceeds over  $Ga<sup>+</sup>$ . The initial step of C–H activation is the oxidative addition of an alkane molecule to the  $Ga<sup>+</sup>$  cation, which proceeds via an indirect heterolytic mechanism involving the basic oxygen atoms of the zeolite lattice. Although the catalytic reaction can also occur over  $\rm{GaH_2}^+$  and  $\rm{GaH}^{+2}$  sites, these paths are not favored. Decomposition of GaH<sub>2</sub><sup>+</sup> leading to formation of Ga<sup>+</sup> during the catalytic cycle is more favorable than regeneration of these sites. The reactivity of GaH $+2$  ions is strongly dependent on the distance between the stabilizing aluminum-occupied oxygen tetrahedra. In cases of greater Al–Al distances, the stability of the GaH<sup>+2</sup> species is very low, and it decomposes to  $Ga<sup>+</sup>$  and a Brønsted acid site, whereas when Al atoms are located more closely, the charge-compensating GaH $^{+2}$  ions are the most stable and exhibit the lowest activity for the initial C–H bond cleavage reaction. © 2006 Elsevier Inc. All rights reserved.

*Keywords:* Zeolite; Gallium; ZSM-5; Alkane dehydrogenation; DFT calculations; Oxidative addition

# **1. Introduction**

Gallium- and zinc-exchanged H-ZSM-5 zeolites (Ga/ZSM-5 and Zn/ZSM-5) are known to be effective catalysts for promoting the selective conversion of light alkanes to aromatics [\[1\].](#page-10-0) The reaction mechanism is thought to consist of a complex scheme involving dehydrogenation, oligomerization, and ringclosure steps [\[2–16\].](#page-10-0) The modifying cations play key roles in dehydrogenation of paraffins [\[2–5,14–16\],](#page-10-0) whereas Brønsted acid protons catalyze the oligomerization of the olefins thus produced and possibly their subsequent aromatization. Numerous experimental [\[2–16\]](#page-10-0) and theoretical [\[17–22\]](#page-10-0) studies have been devoted to investigating the mechanism of catalytic dehydrogenation of light alkanes over gallium-exchanged ZSM-5 zeolites. However, the structure of the active intrazeolite Ga species and, accordingly, the mechanism of hydrocarbon activation have not been fully elucidated.

Extra-framework gallium is introduced into zeolites by either a conventional ion-exchange technique or solid-state ion exchange. In both cases, gallium is initially deposited on the external surface of the zeolite crystals, because hydrated  $Ga^{+3}$ ions are too bulky to enter the elliptical channels of ZSM-5 [\[23\].](#page-10-0) The  $Ga<sub>2</sub>O<sub>3</sub>$  species obtained after calcination are reduced during pretreatment with hydrogen or with the hydrocarbon feed to Ga2O species that migrate into the zeolite channels [\[11,12\].](#page-10-0) These mobile species react with the zeolitic Brønsted acid protons, resulting in formation of reduced cationic  $Ga<sup>+</sup>$ ,  $GaH<sub>2</sub><sup>+</sup>$ , or  $GaH^{+2}$  species bound to zeolite oxygen atoms. The resulting material may contain several types of reduced Ga species besides gallium oxide particles if the reduction process is not complete. The oxide species may include bulkier aggregates on the external surface or smaller ones in the micropore space of the zeolite. Meitzner et al. [\[11\]](#page-10-0) found using in situ Ga K-edge X-ray absorption spectroscopy that in the working catalyst gal-

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<sup>0021-9517/\$ –</sup> see front matter © 2006 Elsevier Inc. All rights reserved. [doi:10.1016/j.jcat.2006.03.011](http://dx.doi.org/10.1016/j.jcat.2006.03.011)

lium is present in reduced  $Ga<sup>+</sup>$  form, although the oxidation state changes to  $3+$  on cooling to lower temperatures. Simi-larly, Kazansky et al. [\[15\]](#page-10-0) found that  $Ga<sup>+</sup>$  species are the most stable species at high temperatures and that oxidative addition of hydrogen to  $Ga^+$  leads to  $GaH_2^+$  species at lower temperatures. It is important to note that these gallium hydride species are relatively stable and decompose only slowly at higher temperatures [\[15\].](#page-10-0)

Recently, a new and completely anhydrous route for the preparation of well-defined cationic Ga species via chemical vapor deposition of trimethylgallium to anhydrous HZSM-5 has been reported [\[14–16,24–26\].](#page-10-0) Careful removal of the methyl ligands by reduction leads to  $GaH_2^+$  cations, which can then be decomposed at high temperatures to  $Ga<sup>+</sup>$  cations. When  $Ga<sup>+</sup>$ cations are predominant in ZSM-5, stable activity in propane dehydrogenation to propylene is observed [\[16\].](#page-10-0) Decreased activity is found when the catalyst contains  $GaH_2$ <sup>+</sup> cations. The higher activity at steady state is attributed to the decomposition of less active  $\text{GaH}_2^+$  cations to  $\text{Ga}^+$  under the reducing high-temperature reaction conditions.

Most theoretical studies have considered  $GaH_2$ <sup>+</sup> as the active site for alkane dehydrogenation [\[17,18,21,22\].](#page-10-0) Frash and van Santen [\[17\]](#page-10-0) proposed a three-step mechanism including (i) "alkyl" ( $R^{\delta-}-H^{\delta+}$ ) activation of the C–H bond, resulting in the formation of a zeolitic Brønsted acid proton and a rather unstable neutral  $H_2Ga-R$  species; (ii) the subsequent desorption of molecular hydrogen via recombination of the acidic proton and one of the hydride ions bounded to gallium; and (iii) the decomposition of the resulting  $[H-Ga-R]^{+}$  complex to alkene and  $GaH_2^+$ . The decomposition step is rate-limiting, and an activation energy of 254 kJ*/*mol is computed for a model reaction of ethane dehydrogenation. Alternatively, a one-step concerted mechanism over  $GaH_2$ <sup>+</sup> was recently considered by Pereira and Nascimento [\[21\].](#page-10-0) The activation energy for this process is substantially higher (by 90 kJ*/*mol) than the mechanism proposed by Frash and van Santen [\[17\]](#page-10-0) and, consequently, this mechanism is less likely. Very recently, Joshi and Thomson [\[22\]](#page-10-0) proposed the existence of bivalent extra-framework gallium species  $(GaH^{+2})$  close to a pair of tetrahedral framework Al species in ZSM-5 zeolite as active sites for alkane dehydrogenation. The overall activation energy for the "carbenium" pathway for ethane activation over  $GaH^{+2}$  species, which are stabilized by two aluminum-containing oxygen tetrahedra, lie in the range of 260–360 kJ*/*mol, depending on the cation site at which  $GaH^{+2}$  species were stabilized. Moreover, the choice for a positively charged alkyl group for the initial activation of ethane contrasts with earlier proposals.

The recent experimental results indicating that  $Ga<sup>+</sup>$  cations are the active sites [\[14–16\]](#page-10-0) led us to reconsider the reaction mechanism of alkane activation over reduced Ga cations stabilized in zeolites. Here we present a detailed comparative analysis of the reactivity of various cationic species  $(Ga^{+}, GaH_{2}^{+},$ and  $GaH^{+2}$ ) by density functional theory (DFT) cluster calculations. In addition, we discuss the relative stability of the various cationic Ga species and the dependence of their chemical properties on the aluminum distribution in ZSM-5 zeolite.

## **2. Experimental**

Dehydrogenation of ethane over Ga/ZSM-5 zeolite, as well as stability of different gallium-containing active sites, was studied using  $GaHAl_2Si_6O_9H_{14}$  and  $GaH_3Al_2Si_6O_9H_{14}$  cluster models, which represent two adjacent five rings from the wall of the straight channel of ZSM-5 zeolite.  $Ga^+$ ,  $GaH_2^+$ , and GaH<sup>+2</sup> cations compensated the negative charge of the  $[AIO_2]^$ unit in one ring, whereas for the first two types of cations, the other negative charge in the other ring was stabilized by a proton. Al atoms were placed in T12 and T8 lattice posi-tions [\[27\]](#page-10-0) to model a cation site  $(Z_d)$  with distantly separated anionic sites, whereas the next nearest T12 and T6 lattice positions were occupied with aluminum atoms in the cluster  $Z_s$ . The distance between two aluminum ions was equal to 8.14 Å for the  $Z_d$  cluster model and 4.84 Å for the  $Z_s$  cluster model. Note that the T12 site is located at the cross-section of the straight and sinusoidal channels of ZSM-5; accordingly, the cations stabilized in the vicinity of this site are considered to have the highest accessibility. Therefore, the charge-compensating gallium species were located in the five-ring-containing aluminum at the T12 position. Hydrogen atoms were used to saturate the dangling Si–O bonds at the periphery of the cluster. The starting geometry of the clusters corresponded to the real lattice of the ZSM-5 zeolite corresponding to X-ray diffraction data [\[28\].](#page-10-0)

DFT, with the B3LYP [\[29\]](#page-10-0) hybride exchange-correlation functional, was used to perform all of the calculations. Earlier, the hybride B3LYP method was reported to provide excellent descriptions of various reaction profiles and particularly of geometries, heats of reaction, activation energies, and vibrational properties of various molecules [\[30\].](#page-10-0) Geometry optimization and saddlepoint searches were all performed us-ing the Gaussian 03 program [\[31\].](#page-10-0) The  $6-31G(d,p)$  basis set was used for the exchanged gallium cation and the bridging hydroxyl group, whereas the ethane molecule and the zeolitic oxygen atoms were described by the  $6-311G(d,p)$  basis set. Al and Si atoms of the zeolite framework, as well as the boundary (H∗) hydrogen atoms, were treated by the D95- Dunning/Huzinaga basis set. It was shown earlier that such a compromise is successful for studies of cation-exchanged zeolites [\[32–34\].](#page-11-0)

As described previously [\[32–34\],](#page-11-0) special restrictions on the positions of the boundary H∗ atoms were imposed during the optimization procedure. In short, the structure of the initial zeolite cluster was first constrained to the X-ray diffraction data [\[28\].](#page-10-0) Subsequently, only Si–H∗ and Al–H∗ bond lengths and the position of the gallium ion were optimized, whereas positions of the other atoms, as well as the directions of the bonds, were fixed according to crystallographic data. The positions of the H∗ atoms in all subsequent calculations were then fixed, whereas the positions of the remaining atoms of the cluster were optimized. All of the energies obtained from the DFT calculations used for estimating the reaction heats and activation barriers were corrected for the zero-point energy.

<span id="page-2-0"></span>

Fig. 1. Optimized structures of (a) Ga  $Z_d$ , (b) GaH<sub>2</sub>  $Z_d$ , (c) GaH<sub>2</sub>  $Z_s$ , (d) Ga  $Z_s$ , (e) GaH<sub>2</sub>  $Z_s$ , and (f) GaH  $Z_s$  clusters.

Table 1

Comparison of the optimized bond lengths and distances (Å), charge parameters (Mulliken charge on atom) and relative energies of  $Ga<sup>+</sup>$ ,  $GaH<sub>2</sub><sup>+</sup>$ , and  $GaH<sup>2+</sup>$ species stabilized in cluster model with distantly separated Al atoms ( $Z_d$ ) and with Al atoms located at the next nearest positions ( $Z_s$ )

	$Ga Z_d$	GaH <sub>2</sub> $Z_d$	$GaH Z_d$	$GaZ_s$	GaH <sub>2</sub> $Z_s$	$GaH Z_s$	$Zn Z_d^a$	Zn 5T <sup>b</sup>
$\Delta E$ (kJ/mol)	$\mathbf{0}$	$-24^{\circ}$	$+88$	$-105$	$-115$ °	$-207$	$\overline{\phantom{0}}$	
Distance								
$Ga$ -O1	2.123	2.011	1.949	2.098	2.000	1.977	1.916	1.961
$Ga$ -O <sub>2</sub>	2.130	2.014	1.976	2.192	2.045	2.066	1.973	2.058
$Ga$ -O3	3.792	3.840	2.080	3.349	3.713	2.025	2.081	2.058
$Ga$ -O4	3.802	3.987	2.138	2.937	3.692	2.028	2.019	1.961
Ga-H1		1.562	1.540	$\overline{\phantom{0}}$	1.566	1.549	$\overline{\phantom{0}}$	
Ga-H <sub>2</sub>	-	1.564		$\overline{\phantom{0}}$	1.559			
Charges on								
Ga	0.548	0.632	0.896	0.525	0.622	0.863	0.984	
O <sub>1</sub>	$-1.126$	$-1.128$	$-1.123$	$-1.130$	$-1.128$	$-1.115$	$-1.138$	
O <sub>2</sub>	$-1.142$	$-1.147$	$-1.100$	$-1.128$	$-1.130$	$-1.098$	$-1.149$	
O <sub>3</sub>	$-1.127$	$-1.125$	$-1.116$	$-0.968$	$-0.951$	$-1.127$	$-1.149$	
<b>O4</b>	$-1.086$	$-1.083$	$-1.126$	$-1.144$	$-1.142$	$-1.144$	$-1.139$	
H1		$-0.079$	0.036	$\overline{\phantom{0}}$	$-0.082$	0.014		
H2		$-0.080$	$\qquad \qquad$		$-0.067$			

<sup>a</sup> The geometry and charge parameters for ZnZ<sub>d</sub> model were obtained from Ref. [\[32\].](#page-11-0)<br>
<sup>b</sup> The geometry parameters for Zn ion stabilized at 5T zeolitic ring with next-nearest Al atoms were obtained from Ref. [\[35\].](#page-11-0)<br>
<sup>c</sup> A

 $\Delta E$  for reaction Ga<sup>+</sup>Z<sup>-</sup> + H<sub>2</sub> → GaH<sub>2</sub><sup>+</sup>Z<sup>-</sup>.

## **3. Results**

### *3.1. Structure and properties of active sites*

Fig. 1 displays the optimized structures of  $Ga^+$ ,  $GaH_2^+$ , and  $GaH^{+2}$  ions stabilized in the  $Z_d$  (distantly separated Al ions) and  $Z_s$  (Al ions in the next-nearest positions). Table 1 lists the corresponding optimized Ga–O and Ga–H bond lengths, the atomic charges, and the relative energies. The univalent cations  $Ga<sup>+</sup>$  and  $GaH<sub>2</sub><sup>+</sup>$  are located in close vicinity to one of aluminum atoms (T12) and coordinate to two adjacent oxygen atoms (O1 and O2). The structural parameters show that the Ga–O bonds (Ga–O1 and Ga–O2) between Ga and lattice oxygens are somewhat shorter for the dihydrido-gallyl ion than for the  $Ga<sup>+</sup>$  cation. On the other hand, the  $Ga<sup>-O</sup>$  distances to the other oxygens (Ga–O3 and Ga–O4) of the cluster are shorter in the latter case. This is most likely due to the repulsive interactions of basic oxygen atoms of the zeolite framework with the negatively charged hydride ions in the bonded  $GaH_2$ <sup>+</sup> complex. On the other hand, weak electrostatic interaction of Ga+ ion with remote zeolitic oxygens leads to additional stabilization of the cation. This is also supported by the fact that the increased basicity of O3 and O4 atoms due to exchange of the Si by Al atom at framework T6 position results in a significant decrease of the corresponding Ga–O distances in the Ga  $Z_s$ cluster. The computed Ga–O and Ga–H distances for  $GaH_2$ <sup>+</sup> species stabilized in either  $Z_d$  or  $Z_s$  clusters agree very well with those reported for the dihydrido-gallyl ion in the extended cluster model containing 11 T atoms [\[22\],](#page-10-0) corresponding to the cation site located at the cross-section of the straight and sinu<span id="page-3-0"></span>soidal channels of ZSM-5 zeolite. We infer that the presence of an additional anionic site in our model that is balanced by an acidic proton does not significantly affect the properties of the gallium-containing sites  $(Ga^+$  and  $GaH_2^+)$ .

The bivalent GaH<sup>+2</sup> ion is preferentially located at the  $Z_d$ site [\(Fig. 1c](#page-2-0)) near the Al1 atom and at a rather long distance  $[r(Ga-A12) = 6.857$  Å] from the second anionic site of the cluster. [Table 1](#page-2-0) shows that the GaH $+2$  ion is coordinated by four oxygen atoms, two of which are bonded at a somewhat shorter distance ( $\sim$ 0.2 Å) due to the lower basicity of the oxygen atoms of the silicon-occupied oxygen tetrahedra compared with those of the aluminum-occupied tetrahedra. This is in agreement with the fact that the GaH $+2$  ion sits almost in the center (Ga–Al1 and Ga–Al2 distances are equal to 2.995 and 2.957 Å, respectively) of the 5T rings containing two anionic sites (GaH  $Z_s$ structure; [Fig. 1f](#page-2-0) ).

The Lewis acidic properties of the  $GaH^{+2}$  ions should be similar to those of  $\text{Zn}^{+2}$ , and, accordingly, we would expect similar bonding properties of these charge-compensating ions with the zeolite. Indeed, the Zn–O bond lengths [\(Table 1\)](#page-2-0) reported by Zhidomirov et al. [\[32–34\]](#page-11-0) for zinc stabilized at the similar cationic site cohere well with the geometry parameters of the GaH  $Z_d$  cluster, taking into account the slightly smaller radius of the Ga<sup>3+</sup> cation. The geometry of the GaH  $Z_s$  correlates also very well with that reported by Shubin et al. [\[35\]](#page-11-0) for zinc ions stabilized in the 5T zeolitic ring containing two alu-minum atoms [\(Table 1\)](#page-2-0). Therefore, one expects the  $GaH^{+2}$  ions to exhibit similar chemical properties to those of exchanged zinc ions.

Desorption of  $H_2$  from  $Gal_2^+(1)$  resulting in formation of  $Ga<sup>+</sup>$  ions is slightly endothermic [\(Table 1\)](#page-2-0). However, due to increase of entropy at high temperature, the equilibrium of this process is shifted strongly toward Ga<sup>+</sup> formation ( $\Delta G^{\circ}_{823 \text{ K}}$  = −75 and −101 kJ/mol, respectively, for Z<sub>d</sub> and Z<sub>s</sub> models). This finding corresponds well to the experimental observation that charge-compensating  $Ga<sup>+</sup>$  ions are transformed into dihydrido-gallyl ions only at lower temperatures in hydrogen atmosphere [\[11,15\].](#page-10-0) Dehydrogenation of these species, resulting in formation of univalent gallium ions, was found to proceed on high-temperature treatment in inert atmosphere or in vacuum [\[15\],](#page-10-0)

$$
GaH_2^+Z^- \rightleftarrows Ga^+Z^- + H_2. \tag{1}
$$

Formation of  $GaH^{+2}$  ions from  $Ga^{+}$  and a Brønsted acid proton (2) is found to be a strongly endothermic process ( $\Delta E =$  $+88$  kJ/mol) for the case of a long Al–Al distance ( $Z_d$  mode) and a strongly exothermic process ( $\Delta E = -102$  kJ/mol) when two Al atoms are placed at the next-nearest positions of the cation site [\(Table 1\)](#page-2-0),

$$
Ga^{+}Z^{-} + H^{+}Z^{-} \rightleftarrows Z^{-} + GaH^{+2}Z^{-}.
$$
 (2)

Therefore, we predict that for relatively long Al–Al distances, the equilibrium of reaction (2) shifts to the side of the univalent  $Ga<sup>+</sup>$  ion and the proton. On the other hand, when located in the vicinity of two anionic sites, the bivalent GaH $+2$  ion is more stable (by 102 kJ/mol) than the  $Ga<sup>+</sup> Z<sub>s</sub>$  site [\(Table 1\)](#page-2-0),

and the equilibrium will shift to the formation of the gallium monohydride.

# *3.2. Ethane dehydrogenation over Ga*+

In agreement with recent experimental DRIFTS investiga-tions [\[14\],](#page-10-0) molecular adsorption of ethane on Ga  $Z_d$  does not result in any specific interaction between  $C_2H_6$  and the adsorption site at low temperature. The geometry and charge properties of both the  $C_2H_6$  moiety and the cluster model in the adsorption complex are similar to those calculated for the individual fragments. Recent experiments [\[15\]](#page-10-0) indicate that at moderate temperature (523 K), dehydrogenation of ethane over Ga/ZSM-5 zeolite is initiated by dissociative adsorption of  $C_2H_6$  on charge-compensating reduced  $Ga^+$  species, resulting in the formation of gallium-ethyl hydride according to

$$
Ga^{+}Z^{-} + C_{2}H_{6} \rightarrow [H-Ga-C_{2}H_{5}]^{+}Z^{-}.
$$
 (3)

Reaction (3) as written corresponds to an oxidative addition of ethane to  $Ga<sup>+</sup>$ , resulting in oxidation of the univalent gallium to  $Ga^{+3}$ . The activation energy of the direct homolytic cleavage of the C–H bond of an ethane molecule on the Ga  $Z_d$  cluster is computed as 374 kJ*/*mol [\[Fig. 2,](#page-4-0) route (a), **TS1** ]. This barrier is too high to explain the experimentally observed formation of  $[C_2H_5-Ga-H]^+$  species (II) at 523 K. Moreover, the value for the activation energy is very close to the C–H bond energy in molecular ethane (423 kJ*/*mol [\[36\]\)](#page-11-0). Thus, it appears that for the case of ethane activation over  $Ga^+$ -exchanged ZSM-5, stabilization of the nonpolar transition state (**TS1** ) is very weak, and most likely the role of the active site is limited to stabilize the products of the homolytic dissociation of ethane via chemisorption of  $C_2H_5$  and H radicals.

Generally, alkanes are activated over transition metal com-plexes [\[37–39\]](#page-11-0) via formation of a  $\sigma$ -C<sub>2</sub>H<sub>6</sub> complex. The bonding of a hydrocarbon molecule with the transition metal ion in such complexes is described by a synergetic combination of the ligand-to-metal donation from the *σ* C–H orbitals of the hydrocarbon to the partially occupied s-orbital of the transition metal (TM) and the metal-to-ligand back-donation from the  $d_{\pi}$  orbital to the C–H  $\sigma^*$ -orbitals. Such interactions result in a very strong weakening of the C–H bond, which in turn, together with formation of new TM*...*C and TM*...*H bonds, significantly facilitates homolytic C–H bond cleavage. However, the fully occupied 3d-orbitals of univalent gallium are of too-low energy and thus do not contribute to the backdonation. Moreover, because the 4s-orbital is occupied, it will not act effectively as an electron-acceptor orbital. Thus, the formation of the *σ* CH complex between ethane and  $Ga<sup>+</sup>$  is unlikely, and, correspondingly, the energy cost for the homolytic dissociation of ethane over Ga  $Z_d$  is very close to that for the gas-phase dissociation.

Alternatively, the interaction with a soft Lewis acid–base pair consisting of  $Ga<sup>+</sup>$  and the basic oxygen atom of the zeolite lattice appears to be responsible for the initial C–H bond cleavage. This route of heterolytic activation of the C–H bond is shown in [Fig. 2,](#page-4-0) route (b). The geometry and charge parameters of the intermediates and transition-state structures are summarized in [Table 2.](#page-4-0) In the initial step, heterolytic dissociation of the

<span id="page-4-0"></span>

Fig. 2. Homolytic (a) and heterolytic (b) "alkyl" pathways of ethane dehydrogenation over Ga Z<sub>d</sub> site.

Table 2 Optimized bond lengths ( $\hat{A}$ ), charges parameters (Mulliken charge on atom) of the intermediates along homolytic and heterolytic reaction paths on Ga  $Z_d$  site

	Ga $Z_{d} + C_{2}H_{6}^{a}$	TS1'	TS1	1	TS <sub>2</sub>	П	TS3
Distance							
$Ga$ -O1	2.123	2.030	3.060	3.188	2.848	2.029	2.130
$Ga$ -O2	2.130	2.047	2.421	2.897	2.227	2.039	2.135
$Ga-C1$	-	2.204	2.226	2.041	2.017	1.984	2.280
Ga-H1	$\overline{\phantom{0}}$	1.804	2.426	2.289	1.792	1.569	1.993
$O1-H1$	-		1.037	1.007	1.257	-	
$Cl-H1$	1.094	1.834	1.757			$\overline{\phantom{0}}$	
$C2-H2$	-	-	-	$\qquad \qquad$	$\overline{\phantom{0}}$	1.094	1.604
$H1-H2$	-		$\overline{\phantom{0}}$	—		3.361	0.871
Charges on							
Ga	0.548	0.341	0.282	0.187	0.262	0.700	0.592
O <sub>1</sub>	$-1.126$	$-1.106$	$-0.992$	$-0.928$	$-1.028$	$-1.125$	$-1.099$
O <sub>2</sub>	$-1.142$	$-1.138$	$-1.156$	$-1.142$	$-1.142$	$-1.145$	$-1.047$
C <sub>1</sub>	$-0.317$	$-0.327$	$-0.639$	$-0.449$	$-0.432$	$-0.457$	$-0.417$
H1	0.106	$-0.063$	0.461	0.378	0.338	$-0.075$	$-0.032$
C <sub>2</sub>	-		-	$\qquad \qquad -$		$-0.284$	$-0.261$
H <sub>2</sub>	$\qquad \qquad$					0.111	0.051

<sup>a</sup> For isolated C<sub>2</sub>H<sub>6</sub> molecule distances and charges were computed at B3LYP DFT level with 6-311G(d,p). For isolated C<sub>2</sub>H<sub>4</sub> molecule Mulliken charges computed at the same level are −0.219 and 0.109 on C and H atoms, respectively.

C–H bond results in formation of a neutral  $Ga-C<sub>2</sub>H<sub>5</sub>$  species in the vicinity of a zeolitic Brønsted acid site (**I**). The calculated activation energy (**TS1**, 210 kJ*/*mol) is significantly lower than that obtained for the homolytic path. The corresponding transition state structure (**TS1**) is characterized by very strong polarization of the reacting C–H bond following the "alkyl" mechanism; that is, both the positive charge on the H atom and the negative charge on carbon strongly increase compared with gas-phase  $C_2H_6$ . At the same time, the positive charge on the gallium decreases, indicating weakening bonds between the cation and zeolitic oxygen. The partial negative charge on the O1 atom also decreases due to bonding with the proton from ethane. Similar effects were also observed for the O3 atom of the  $Z_s$  cluster model [\(Table 1\)](#page-2-0) for the Ga  $Z_s$  and GaH<sub>2</sub>  $Z_s$  clusters.

The intermediate (**I**) resulting from heterolytic activation of ethane over the Ga  $Z_d$  site is very unstable and readily rearranges to the stable product (**II**). This reaction proceeds via oxidation of the  $Ga-C<sub>2</sub>H<sub>5</sub>$  species by the Brønsted acid site with a very low activation barrier (9 kJ*/*mol, **TS2**). The ease of formation of complex (**II**) also explains why only the product of oxidative addition was observed experimentally [\[15\].](#page-10-0)

The final step in ethane dehydrogenation over  $Ga<sup>+</sup>$  was found to be a one-step desorption of  $H_2$  and  $C_2H_4$  molecules via the **TS3** structure. This reaction can be described as a "destructive reductive elimination," resulting in reduction of the  $Ga^{+3}$ 

<span id="page-5-0"></span>ion and regeneration of the initial Ga  $Z_d$  site. [Table 2](#page-4-0) shows that the hydrogen atoms of the free methyl group in structure **II** are positively charged, whereas the H atom bounded to gallium is negatively charged. Hence, the catalytic cycle is closed by the recombination of these atoms to form molecular hydrogen via transition state **TS3**. The activation barrier of the latter process is computed as 224 kJ*/*mol. This value is slightly higher than that calculated for the initial C–H cleavage (210 kJ*/*mol). The overall activation energy of the ethane dehydrogenation over the reduced dehydrogenated Ga/ZSM-5 zeolite is 233 kJ*/*mol.

# *3.3. Ethane activation over GaH2* +

To compare the reactivities of the various charge-compensating gallium species, we investigated the alkyl activation pathway over the  $GaH_2$ <sup>+</sup> site proposed by Frash and van Santen  $[17]$  with the present  $Z_d$  cluster model. The energetics for this mechanism are presented in [Fig. 3,](#page-6-0) and the geometry and charge parameters of the intermediates and transition-state structures are listed in [Table 3.](#page-6-0)

Similar to the findings for  $Ga^+$ , molecular adsorption of ethane on the dihydrido-gallyl ion stabilized in the  $Z_d$  cluster was very weak and did not result in any significant perturbation of either the adsorbed molecule or the adsorption site. Thus, it is assumed that this molecular adsorption does not influence the subsequent chemical activation of  $C_2H_6$  molecules. The mechanism of the initial activation of the hydrocarbon molecule on dihydrido-gallyl ion is very similar to that suggested for the heterolytic dissociation of ethane on Ga  $Z_d$ . Indeed, a very strong polarization of the reacting C–H bond is observed in the **TS4** structure, leading to heterolytic C–H bond splitting with formation of a neutral  $(H^-)$ <sub>2</sub> $Ga^{+3}$ - $C_2H_5$ <sup>-</sup> species in the vicinity of a Brønsted acid site (**III**). The calculated activation energy for this elementary step (193 kJ*/*mol) is significantly higher than that  $(158 \text{ kJ/mol})$  reported previously  $[17]$  for  $\text{GaH}_2^+$  species stabilized in a fully optimized 3T cluster. On the other hand, the present value is slightly lower than that (203 kJ*/*mol) reported by Yoshi and Thomson [\[22\]](#page-10-0) for the dihydrido-gallyl ion stabilized at a more extended cluster model containing 11T atoms. We attribute the higher activation barrier than that reported by Frash and van Santen [\[17\]](#page-10-0) mainly to greater steric hindrance of the interaction of the C–H bond with the Ga*...*O pair caused by the constrained geometry and the larger size of the cluster model. The difference between the present result and that reported in [\[22\]](#page-10-0) is also attributed to the steric factors and to different basic properties of the zeolitic O atom involved in the C–H activation resulting from size differences of the cluster model.

The  $H_2Ga-C_2H_6$  species formed in the initial step are stabilized by interaction between a hydride ion (H1 ) bonded to the gallium and an acidic proton (H1). This interaction results in a strong elongation (by about 0.2 Å) of the O1–H1 bond. The Ga–O2 distance in structure **III** [\(Table 3\)](#page-6-0) is significantly less than the corresponding distance in structure **I** [\(Table 2\)](#page-4-0) and is indicative of the stronger interaction of the trivalent gallium in the  $H_2Ga-C_2H_6$  species with the framework zeolitic oxygens. Due to the latter interaction, the coordination of the  $Ga^{+3}$  ion

in structure **III** is rather close to tetrahedral, which is known to be preferred for  $Ga^{+3}$ -containing compounds [\[40\].](#page-11-0) Thus, both attractive interactions provide additional stabilization of the reactive species **III** compared with  $Ga-C<sub>2</sub>H<sub>6</sub>$  species (**I**). Moreover, this facilitates subsequent decomposition of **III** via desorption of  $H_2$  and formation of the stable tetrahedral gallium in the  $[H-Ga-C<sub>2</sub>H<sub>5</sub>]<sup>+</sup>$  ion (**II**). The calculated activation barrier (**TS5**) for this process is equal to 2 kJ*/*mol.

To close the catalytic cycle via regeneration of the initial dihydrido-gallyl ion, the decomposition of the structure **II** was proposed by Frash and van Santen to proceed via abstraction of a hydride ion from the *β*-position of the ethyl group by the positively charged gallium atom and simultaneous desorption of ethylene [\[Fig. 3,](#page-6-0) route (a)]. The activation energy for this process was 257 kJ*/*mol, in an excellent agreement with the previously reported values of 258 kJ*/*mol [\[22\]](#page-10-0) and 254 kJ*/*mol [\[17\].](#page-10-0) This close agreement indicates that the chemical properties of the exchanged trivalent gallium species almost do not depend on the surrounding unless the other atoms of the zeolite are involved in the reaction. However, [Table 3](#page-6-0) shows that both the abstracting H atom of the *β*-methyl group and the gallium ion are positively charged. Thus, regeneration of the  $GaH<sub>2</sub>$ <sup>+</sup> active site requires "repolarization" of the C–H bond, a process that appears to be unfavorable. On the other hand, simultaneous desorption of  $H_2$  and  $C_2H_4$  [\[Fig. 3,](#page-6-0) route (b)], which results in formation of the univalent gallium ion (Ga  $Z_d$ ), is about 30 kJ/mol more favorable than closure of the cycle with regeneration of the dihydrido-gallyl ion. Note that this process is also strongly favored because of the entropy factor. The calculated Gibbs energy changes  $(\Delta G_{823}^\circ)$  at the conditions of catalytic reaction (823 K, 1 atm.) are equal to  $+1$  for route (a) and −74 kJ*/*mol for route (b).

# *3.4. Ethane activation over GaH*+*<sup>2</sup>*

Recently, Joshi and Thomson [\[22\]](#page-10-0) proposed that the GaH<sup>+2</sup> species stabilized in the vicinity of two framework Al atoms are the active species for hydrocarbon dehydrogenation in Ga/ZSM-5 catalysts. The initial step of alkane activation over these active sites was suggested to be a heterolytic dissociation of the C–H bond via a "carbenium" mechanism, resulting in formation of a "carbenium" ion attached to the basic oxygen of the zeolite and a hydride ion bonded to gallium (GaH  $Z_d + C_2H_6$ )  $\rightarrow$  V) [\[Fig. 4,](#page-7-0) route (a)]. In view of earlier results [\[17,41\],](#page-10-0) this mechanism seems disputable. Thus, to clarify the mechanism of alkane activation over  $GaH^{+2}$  species and to compare the reactivity with those of the earlier discussed gallium containing sites, the initial activation of ethane over  $GaH^{+2}$  stabilized at the  $Z_d$  cluster was computed.

The elementary steps and the reaction energy diagrams for the "carbenium" and "alkyl" pathways of ethane activation over GaH  $Z_d$  cluster are shown in [Fig. 4,](#page-7-0) routes (a) and (b), respectively. The geometry and charge parameters of the intermediates and transition state structures involved are summarized in [Table 4.](#page-7-0) According to Joshi and Thomson [\[22\],](#page-10-0) activated molecular adsorption of ethane on  $GaH^{+2}$  species (structure **IV** in [Fig. 4\)](#page-7-0) precedes C–H bond cleavage. In contrast to the

<span id="page-6-0"></span>

Fig. 3. Reaction paths for the "alkyl activation" mechanism of ethane dehydrogenation (a) over GaH<sub>2</sub>  $Z_d$  and dehydrogenation of these species in the catalytic cycle (b) resulting in formation of Ga  $Z_d$ .





aforementioned molecular adsorption of  $C_2H_6$  on Ga  $Z_d$  and  $GaH<sub>2</sub>$   $Z<sub>d</sub>$ , this process leads to very significant changes in the geometry and charge parameters of both adsorbed  $C_2H_6$ and the adsorption site. The Ga–O coordination opens (Ga– O3 and Ga–O4 bonds are broken), and the GaH $+2$  ion partially leaves the cation site (5T ring), so that gallium becomes coordinated to only two framework oxygens (O1 and O2). The coordinative unsaturation of the GaH $+2$  species is then partially compensated by interaction with one of the methyl group of ethane. Formation of such an activated adsorption complex is a strongly endothermic process (GaH  $Z_d + C_2H_6 \rightarrow IV$ ,  $\Delta E =$ +68 kJ*/*mol; [Fig. 4\)](#page-7-0), because it requires destruction of a stable fourfold coordination of GaH by the lattice oxygen atoms. On the other hand, coordination of ethane to the cation does not

<span id="page-7-0"></span>

Fig. 4. "Alkyl" (a) and "carbenium" (b) activation of ethane over GaH  $Z_d$ .

Table 4 Optimized bond lengths (Å), charges parameters (Mulliken charge on atom) of the intermediates involved in the initial activation of ethane on GaH  $Z<sub>d</sub>$  site

	GaH <sub>2</sub> $Z_{d} + C_{2}H_{6}$	IV	V	TS6	VI
Distance					
$Ga$ -O1	1.949	1.948	2.058	2.000	2.112
$Ga$ -O2	1.976	1.872	1.979	1.924	1.992
$Ga$ -O3	2.080	3.470	3.615	3.400	3.722
$Ga$ -O4	2.138	3.882	4.372	3.349	4.538
$Ga-H1'$	1.540	1.533	1.552	1.552	1.559
$Ga-C1$		2.566		2.145	1.997
$Ga-H1$		2.027	1.571	2.371	
$O4-C1$		3.295	1.543	2.664	
$O4-H1$		2.418		1.201	0.980
$C1-H1$	1.094	1.132	3.172	1.505	3.441
Charge on					
Ga	0.896	0.781	0.638	0.682	0.635
O1	$-1.123$	$-1.107$	$-1.117$	$-1.128$	$-1.119$
O <sub>2</sub>	$-1.100$	$-1.105$	$-1.149$	$-1.141$	$-1.148$
O <sub>3</sub>	$-1.116$	$-1.160$	$-1.142$	$-1.161$	$-1.139$
O4	$-1.126$	$-1.126$	$-0.954$	$-1.074$	$-0.916$
H1'	0.036	0.057	$-0.009$	0.021	$-0.002$
C1	$-0.317$	$-0.411$	$-0.069$	$-0.651$	$-0.413$
H1	0.106	0.218	$-0.154$	0.527	0.408

compensate for the energy loss associated with the breaking of two Ga–O bonds (Ga–O3 and Ga–O4). In other words, it is not possible to form a strong adsorption complex of ethane with GaH  $Z_d$  without decreasing the effective coordination number of the cation to the basic zeolitic oxygens, as was observed for  $\text{Zn}^{+2}$  ion stabilized in a similar cluster model [\[32,33\].](#page-11-0) The difference with  $GaH^{+2}$  is that the gallium ion in the initial  $GaH$  $Z_d$  model is shielded by the attached hydride ion, which hinders the stabilizing charge donation from ethane to the cation. The twofold coordination of  $GaH^{+2}$  ion in structure **IV** removes these hindrances. The effective transfer of electron density from ethane to the adsorption site is 0*.*283e−, which is in agreement with the significant decrease in the positive charge of the



Fig. 5. Calculated IR frequencies of C–H stretching vibrations with their intensities and simulated IR spectrum (with all DFT computed vibrational frequencies scaled by factor 0.964) for structure **IV**. The shape of the C–H vibration mostly perturbed due to interaction with  $GaH^{+2}$  ion is shown by "balls and sticks" model. IR spectrum of free  $C_2H_6$  molecule calculated at B3LYP/6-311G(d,p) level is presented for comparison by the dashed line.

 $GaH^{+2}$  ion (Table 4). This indicates appreciable Lewis acidity of the "activated"  $GaH^{+2}$  ion in a cationic position with distantly placed aluminum ions. The charge transfer is much larger (by 0*.*168e−) than that for ethane adsorption on zinc ions [\[32\],](#page-11-0) indicating a much stronger Lewis acidity of low-coordinated  $GaH^{+2}$  species.

Interaction of the hydrocarbon molecule with the excessively charged low-coordinated monohydrido-gallyl ion results in very strong polarization of the adsorbed molecule. This is reflected in a very strong increase in the negative charge on the carbon atom (C1) and, at the same time, of the positive charge on the hydrogen atom (H1) involved in the interaction (Table 4). In addition, the C1–H1 bond length is 0.038 Å longer than that of the corresponding value for gas-phase ethane. These perturbations of the adsorbed molecule affect the vibrational properties of the  $C_2H_6$  moiety in structure **IV** (Fig. 5). One can see that the calculated IR spectrum of C–H vibrations of **IV** contains five slightly perturbed bands with frequencies close to those observed in the gas phase, whereas one band is very

	$\frac{1}{2}$			
	$E_{\text{act}}$ (kJ/mol)	$\Delta E$ (kJ/mol)		
$GaZ_s$				
"Homolytic" path				
$Ga^{+}Z^{-} + C_{2}H_{6} \rightarrow [H-Ga-C_{2}H_{5}]^{+}Z^{-}$	$+386$	$+23$		
"Heterolytic" path				
$Ga^{+}Z^{-} + C_{2}H_{6} \rightarrow Ga-C_{2}H_{5}H^{+}Z^{-}$	$+219$	$+194$		
Ga–C <sub>2</sub> H <sub>5</sub> H <sup>+</sup> Z <sup>–</sup> $\rightarrow$ [H–Ga–C <sub>2</sub> H <sub>5</sub> ] <sup>+</sup> Z <sup>–</sup>	$\qquad \qquad$	$-171$		
GaH $Z_s$				
"Alkyl" path				
$Z^-$ GaH <sup>+2</sup> $Z^-$ + C <sub>2</sub> H <sub>6</sub> $\rightarrow$ [H–Ga–C <sub>2</sub> H <sub>5</sub> ] <sup>+</sup> $Z^-$ + H <sup>+</sup> Z <sup>–</sup>	$+252$	$+125$		
"Carbenium" path				
$Z^-$ GaH <sup>+2</sup> $Z^-$ + C <sub>2</sub> H <sub>6</sub> $\rightarrow$ [H–Ga–H] <sup>+</sup> $Z^-$ + C <sub>2</sub> H <sub>5</sub> <sup>+</sup> $Z^-$	$\overline{\phantom{m}}$	$+274$		

Table 5 Energetics of initial activation of ethane over  $Ga^+$  and  $GaH^+2$  sites based on Ga Zs and GaH Zs models, respectively

strongly red-shifted (by  $>300 \text{ cm}^{-1}$ ) and exhibits a very high relative intensity compared with those of the other C–H stretching bands. This band corresponds mainly to displacement of the hydrogen atom (H1) for the C1–H1 bond directly interacting with the GaH<sup>+2</sup> ion. Recently we reported that such a strong perturbation of adsorbed molecules leads to their subsequent chemical activation at higher temperatures after the displacement of atoms of the adsorbed molecule corresponding to the most intense low-frequency infrared band [\[42\].](#page-11-0) Thus, the initially proposed structure for the product of C–H activation of ethane on GaH  $Z_d$  was built by displacement of the H1 atom by 1 Å in structure **IV** following the aforementioned C–H stretching vibration. Geometry optimization of the resulting structure leads to formation of product **VI** of the "alkyl" heterolytic C–H bond cleavage. The calculated activation energy for this process  $[IV \rightarrow VI; Fig. 4, route (b)]$  $[IV \rightarrow VI; Fig. 4, route (b)]$  $[IV \rightarrow VI; Fig. 4, route (b)]$  is equal to 104 kJ/mol. The corresponding transition state structure **TS6** is characterized by an increase in the "alkyl" C1–H1 bond polarization, resulting in formation of a proton  $(H^+)$  attached to the basic zeolitic O atom and an alkyl  $(C_2H_5^-)$  grafted to the gallium ion. The resulting product, **VI**, is destabilized due to localization of likely charged ions (H<sup>+</sup> and [H–Ga–C<sub>2</sub>H<sub>5</sub>]<sup>+</sup>) in the immediate vicinity of one another. However, it can be further stabilized by 195 kJ*/*mol via proton transfer from O4 (structure **IV**) to the more basic O7 ion bounded to the Al2 (structure **II**). It was shown previously [\[34\]](#page-11-0) that the activation energy of this process does not exceed 50 kJ*/*mol.

It was also found that the product (**V**) of "carbenium" activation of  $C_2H_6$  on GaH  $Z_d$  is just 14 kJ/mol less stable than structure **VI [**[Fig. 4](#page-7-0) routes (a) and (b), respectively]. Unfortunately, we could not locate the transition-state structure corresponding to the "carbenium" mechanism of ethane activation on GaH<sup>+2</sup> species  $[IV \rightarrow V; Fig. 4, route (a)]$  $[IV \rightarrow V; Fig. 4, route (a)]$  $[IV \rightarrow V; Fig. 4, route (a)]$  proposed by Joshi and Thomson [\[22\].](#page-10-0) However, with regard to the above discussion, it is obvious that this process will be less favorable than the "alkyl" one, because reaction  $IV \rightarrow V$  requires very strong "repolarization" of the electron density of adsorbed ethane to produce a negative charge on H1 and a positive charge on the carbon atom (C1). There do not appear to be any facilitating factors for this process, and hence we surmise that the "carbenium" pathway will be strongly disfavored in comparison with the "alkyl" activation of ethane on charge-compensating  $GaH^{+2}$  sites.

Thus, the initial activation of  $C_2H_6$  on GaH  $Z_d$  results in formation of the intermediate **II**, and hence, the catalytic cycle follows the reaction pathway described for ethane dehydrogenation over Ga  $Z_d$  (Section [3.2\)](#page-3-0), and GaH<sup>+2</sup> is converted to  $Ga<sup>+</sup>$ .

# *3.5. Effect of Al–Al distance on the reactivity of Ga*+ *and GaH*+*<sup>2</sup> sites*

The stability and reactivity of  $Ga<sup>+</sup>$  and  $GaH<sup>+2</sup>$  ions in the  $Z_s$ cluster model were compared with those for clusters in which aluminum atoms are separated by a relatively long distance  $(8.138 \text{ Å})$ . Here we present the computational results of ethane activation over these ions compensating for the negative charge in cluster models in which the aluminum ions are placed at the next-nearest allowed framework positions [Ga  $Z_s$  and GaH  $Z_s$ ;  $r(A11-A12) = 4.837 \text{ Å}$ . The intermediates and transition-state structures thus calculated are very similar to those obtained for the  $Z_d$  model and exhibit similar trends in changes of geometry and charge parameters of intermediates due to chemical conversions. The calculated energetic parameters for elementary steps of ethane activation on Ga  $Z_s$  and GaH  $Z_s$  are summarized in Table 5.

The activation energies and enthalpies for both the homolytic and heterolytic C–H bond cleavage on  $Ga^+$  ion in  $Z_s$ clusters are very similar to those calculated for the distantly separated Al atoms. Thus, it can be concluded that relative localization of anionic  $[AIO<sub>2</sub>]<sup>-</sup>$  units in the framework of zeolite does not significantly affect the reactivity of the chargecompensating univalent gallium ions. In contrast, the chemical properties of  $GaH^{+2}$  depend strongly on the Al–Al distance in the cluster used. Similar to Joshi and Thomson [\[22\],](#page-10-0) we could not detect activated molecular adsorption of ethane on GaH Z<sub>s</sub> corresponding to the earlier-considered structure **IV** [\(Fig. 4\)](#page-7-0). This is most likely connected to the fact that  $GaH^{+2}$ ion is much more strongly coordinated with the basic lattice oxygens of  $Z_s$  than with those of  $Z_d$  cluster model. Hence, coordination of ethane with the low-coordinated gallium ion cannot even partially compensate for the loss of energy due to Ga– O bond breaking, which is necessary for the formation of the  $C_2H_6$ ...GaH<sup>+2</sup> activated adsorption complex. This agrees well with a much higher activation barrier for the "alkyl" C–H bond dissociation. As follows from Table 5, the energy cost of the reaction (4) is 42 kJ/mol higher in the GaH  $Z_s$  site than in the GaH  $Z_d$  site,

$$
Z^-GaH^{+2}Z^- + C_2H_6 \to [H-Ga-C_2H_5]^+Z^- + H^+Z. \tag{4}
$$

The transition-state structure for the "carbenium" initial activation of ethane on GaH  $Z_s$  was not identified. However, the enthalpy of this process is equal to +274 kJ*/*mol; therefore, the activation energy would be expected to be higher than this value. This then significantly exceeds the value of the activation energy calculated for the "alkyl" pathway. Taking into account the results of Section [3.4,](#page-5-0) the latter process seems to be more favorable over  $GaH^{+2}$  ions independent of the distance between charge-compensating  $[AIO<sub>2</sub>]<sup>-</sup>$  anionic sites.

## **4. Discussion**

In the present study, we considered three possible types of charge-compensating gallium species in reduced Ga/ZSM-5:  $Ga<sup>+</sup>$ ,  $GaH<sub>2</sub><sup>+</sup>$ , and  $GaH<sup>+2</sup>$ . Stability of univalent species ( $Ga<sup>+</sup>$ ,  $GaH_2$ <sup>+</sup>) is remarkably higher than that of  $GaH_1$ <sup>+2</sup> in the case of low Al content in zeolite, that is, distantly separated framework Al atoms. In contrast, when the Al–Al distance is rather small (with two aluminums located in the next-nearest positions), the presence of bivalent ions is preferred in the immediate vicinity of two anionic sites. The repulsive interaction between two closely situated positively charged univalent species results in strong destabilization of  $Ga<sup>+</sup>$  and  $GaH<sub>2</sub><sup>+</sup>$  at such cation sites.

The fraction of cation sites containing two aluminum atoms in the next-nearest positions is small; for instance, in a zeolite with an Si:Al ratio of 25, it does not exceed 30% [\[43\].](#page-11-0) Thus, with regard to the results presented in [Table 1,](#page-2-0) it can be concluded that univalent  $Ga^+$  or  $GaH_2^+$  ions are the predominant charge-compensating species in high-silica gallium-exchanged zeolites, whereas  $GaH^{+2}$  cations can be found in only a relatively small portion of zeolitic cation sites, which contain two Al atoms.

It was found that at the initial step of ethane activation, all of the gallium species considered act as Lewis acids promoting heterolytic C–H cleavage involving the basic oxygen atoms of the zeolite lattice. In  $Ga^{+}$  and  $GaH_2^{+}$  active sites, this results in the formation of very unstable neutral  $Ga-C<sub>2</sub>H<sub>5</sub>$  and  $H_2Ga-C_2H_5$  species, respectively, as well as a Brønsted acid site, which readily either oxidizes  $Ga-C<sub>2</sub>H<sub>5</sub>$  species or recombines with one of the hydride ions bounded to  $H_2Ga-C_2H_5$ , leading to desorption of hydrogen. In both cases, at the end of the reaction, very stable  $[H-Ga-C<sub>2</sub>H<sub>5</sub>]+Z^-$  species  $(\mathbf{II})$  are formed.

The catalytic cycle is closed by one-step decomposition of  $[H-Ga-C<sub>2</sub>H<sub>5</sub>]<sup>+</sup>Z<sup>-</sup>$ . It was found that simultaneous desorption of  $H_2$  and  $C_2H_4$  from these species [reaction (5)] is the most favorable process. The activation energy for production of  $Ga<sup>+</sup>$ from [H–Ga–C2H5] + following reaction (5) is 33 kJ*/*mol lower than that for regeneration of  $GaH_2$ <sup>+</sup> via desorption of ethylene (6). Moreover, under the conditions of the catalytic process, due to the entropy factor, the  $\Delta G_{823}^{\circ}$  is much lower for reaction (5) than for reaction (6) (−74 vs. +1 kJ*/*mol),

$$
[H-Ga-C_2H_5]^+Z^- \to Ga^+Z^- + C_2H_4 + H_2 \tag{5}
$$

and

$$
[H-Ga-C_2H_5]^+Z^- \to GaH_2^+Z^- + C_2H_4. \tag{6}
$$

Indeed, in reaction (5), rotation of the ethyl group results in formation of some weak attractive interaction between an unlikely charged hydride ion and a H atom from the *β*-methyl group of the  $C_2H_5$ <sup>-</sup> bound to gallium. In contrast, reaction (6) proceeds via abstraction of a hydride ion by a positively charged gallium from the same *β*-methyl group. This process requires significant repolarization of the C–H bond involved and thus exhibits a higher activation barrier. Therefore, ethane dehydrogenation over dihydrido-gallyl ions results in their decomposition. The equilibrium concentration of  $\mathrm{GaH_{2}}^{+}$  at high temperature is very low, and hence these sites cannot be considered responsible for ethane dehydrogenation. This finding is in agreement with the recent experimental results [\[16\]](#page-10-0) indicating decomposition of  $GaH<sub>2</sub><sup>+</sup>$  ions in the catalytic process.

According to the results presented above on the reactivity of  $GAH^{+2}$  species, these species do not play a significant role as active sites in the reaction considered. In addition, the mechanism of ethane activation proposed by Joshi and Thomson [\[22\]](#page-10-0) is disputable. Those authors suggested that gallium in such species acts as a hydride ion acceptor and that the C–H bond polarization follows a "carbenium" mechanism (C*δ*+–H*δ*−); however, the activated molecular adsorption of ethane, which precedes C–H cleavage, results in the opposite C*δ*−–H*δ*<sup>+</sup> polarization. Note that this finding is in line with the higher electronegativity of carbon with respect to hydrogen (2.5 vs. 2.1 in the Pauling scale [\[44\]\)](#page-11-0). It is obvious that subsequent dissociative adsorption of ethane should follow the "alkyl" mechanism leading to formation of the intermediate product [H–Ga–  $C_2H_5$ ]<sup>+</sup>Z<sup>-</sup>.

It is also noticeable that the  $GaH^{+2}$  species are isolobal to  $\text{Zn}^{+2}$  ions. This is reflected in the similarities of both the geometry and the charge properties of the zeolitic cation sites containing corresponding species [\(Table 1\)](#page-2-0), as well as their chemical properties. Recently, it was shown experimentally [\[42,45\]](#page-11-0) and theoretically [\[41\]](#page-11-0) that the "alkyl" pathway of hydrocarbon dehydrogenation over zinc-exchanged zeolites is much more favorable than the "carbenium" pathway. The same conclusion follows directly from the calculations presented for  $GaH^{+2}$  ions exchanged in zeolite independently on the distance between charge-compensating  $[AIO<sub>2</sub>]<sup>-</sup>$  framework units. The reactivity of either  $\text{Ga}^+$  or  $\text{GaH}_2{}^+$  in hydrocarbon activation exhibits very slight dependence on the distribution of aluminum in zeolite. In contrast, the GaH $+2$  stabilized in the cation site containing two anionic sites in the same zeolitic ring is much less active than that in the "charge-alternating" cation site.

Summarizing the foregoing results, we can conclude that univalent  $Ga<sup>+</sup>$  ions at cation sites of high-silica zeolites are the most probable active species for the hydrocarbon dehydrogenation reaction. The apparent activation barrier for this process estimated within the model used is equal to 233 kJ*/*mol. To the best of our knowledge, no experimental data are available on the activation energies for alkane dehydrogenation over well-defined gallium-exchanged zeolites. However, the apparent activation barrier estimated for ethane dehydrogenation over <span id="page-10-0"></span>Ga<sub>2</sub>O<sub>3</sub>/HZSM-5 [\[46\]](#page-11-0) is significantly lower (163 kJ/mol) than this value. This disagreement is most likely due to the imperfection of the model used. Indeed, it does not take into account the electrostatic field of the zeolite cage, which can significantly stabilize polar transition state structures [\[47\]](#page-11-0) involved in this process. Moreover, physical adsorption of ethane (∼20– 30 kJ*/*mol) due to dispersive interactions between the hydrocarbon molecule and zeolitic walls, which cannot be correctly estimated by DFT, also decreases apparent activation energy compared with the true one.

#### **5. Conclusion**

The reaction mechanism of ethane dehydrogenation was investigated using DFT calculations for various reduced-gallium sites in Ga/ZSM-5. The probable catalytic cycle starts with the heterolytic C–H bond cleavage involving exchanged univalent gallium cation and a basic oxygen atom of the zeolite framework. The low energy of the d-orbitals of  $Ga<sup>+</sup>$  and its occupied s-orbital that make them unable to donate or accept electrons, respectively, from the hydrocarbon result in a high barrier for the direct oxidative addition of ethane to the cation. Therefore, heterolytic splitting of the C–H bond is much more favorable due to the polarization induced by the interaction of the hydrocarbon with the Ga*...*O Lewis acid–base pair. The resulting product easily rearranges to form  $[H-Ga-C<sub>2</sub>H<sub>5</sub>]<sup>+</sup>$ , which decomposes via simultaneous desorption of  $H_2$  and  $C_2H_4$ , regenerating the initial  $Ga<sup>+</sup>$  species. The overall activation barrier for C<sub>2</sub>H<sub>6</sub> dehydrogenation over  $Ga^{+}Z^{-}$  sites is equal to 233 kJ*/*mol.

Hydrogenated gallium species (GaH<sub>2</sub><sup>+</sup>Z<sup>-</sup> and Z<sup>-</sup>GaH<sup>+2</sup>Z<sup>-</sup>) are less likely active sites. Decomposition of the dihydridogallyl ions, resulting in formation of univalent gallium ions during the catalytic cycle, is significantly favored over regeneration of  $GaH_2$ <sup>+</sup> sites. In addition, the estimated overall activation barrier for the considered catalytic reaction is higher (by 58 kJ/mol) for  $GaH_2$ <sup>+</sup> sites than for  $Ga$ <sup>+</sup> sites.

Bivalent GaH $+2$  species stabilized at the cation site with distantly separated framework Al sites exhibit significantly higher initial activity for ethane activation but much lower stability compared with  $Ga<sup>+</sup>$  sites. However, initial heterolytic cleavage of the C–H bond results in formation of  $[H-Ga-C<sub>2</sub>H<sub>5</sub>]+$ ions that preferentially follow the reaction path, again leading to univalent gallium cations.

On the other hand,  $GaH^{+2}$  ions charge-compensating two proximate framework aluminum ions are the most stable cationic species; however, initial activation of the C–H bond over these sites is strongly disfavored both thermodynamically and kinetically. In contrast, the reactivity of univalent gallium species exchanged in zeolite depends only slightly on the relative position of zeolitic anionic sites  $([AIO<sub>2</sub>]<sup>-</sup>$  units).

#### **Acknowledgments**

The authors thank Professor G.M. Zhidomirov for fruitful discussions. This work was sponsored by the National Computing Facilities Foundation, which provided supercomputer facilities, with financial support from the Netherlands Organization for Scientific Research (NWO). Support from the Dutch Science Foundation in the collaborative Russian–Dutch research project 047-015-001 NWO is also acknowledged.

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